Proc. Conference on Challenges and Applications of Mathematical Modelling Techniques in Building Science and Technology (CAM2TBST), Central Building Research Institute, Roorkee. February 7-8, 2008

SPREADSHEET APPLICATIONS IN BUILDING MATERIAL RESEARCH STUDIES

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ABSTRACT

Spreadsheets are widely used computer software due to their simplicity and user friendliness. They are available on most of the computers and mainly used for data management, calculation, making charts or statistical analysis. However, their potential in materials research is not fully explored yet. In this paper various applications of spreadsheets in different building material research studies have been presented. Their use particularly in computation of the engineering material properties like strength, modulus, thermal conductivity, heat of hydration; mix design; numerical differentiation & integration; and statistical analysis are described with case studies using Microsoft Excel[™]. The advantages and limitations of the spreadsheets in such applications are also discussed.

INTRODUCTION

A spreadsheet is a computer programme that has several built-in statistical and graphics functions. Microsoft Office Excel is the most commonly used spreadsheet software programme. Lotus 1-2-3, Quattro Pro and Open Office Calc are some other popular spreadsheet programmes. In spreadsheets entering data in the form of numbers or text, and formulae is a quick and simple task. Further they facilitate importing and exporting data, easy calculation, data analysis and graphical presentation with various formats. The capability of the spreadsheets can be further enhanced by various 'add-in' software easily available on the internet as free or commercial products. In addition, numerous worksheet functions can be written as 'macros' that allow combination of different commands. The macros can be either written in a computer language called Visual Basic for Applications (VBA) or recorded. They can be run whenever similar tasks

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have to be executed. This is a very valuable facility for running repetitive tasks. The other feature is that the spreadsheets containing various data can be interlinked.

The use of paper-based spreadsheets is an old practice. They have been used for hundreds of years for keeping records and accounting purposes. However, the use of computer based spreadsheet began from 1979 when Dan Bricklin conceptualise it and Bob Frankston wrote the programme on Apple II platform [1]. Initially, the PC based spreadsheets were written for accounting applications, but with time their use gradually increased in different fields. Nowadays spreadsheets are widely used in laboratory experiments for collecting, storing and analysis of data.

The main reason behind the wider use of spreadsheets is that it is easier and quicker to use a spreadsheet than write a computer program. A person using spreadsheet is not essential to be a computer programmer. Moreover, if some modification is required it is difficult to understand the underneath mathematics in other programmes, while spreadsheets are more convenient. What-If Analysis and Solver are very useful features in Excel spreadsheet. In What-If Analysis the change in output can be assessed for a given change in inputs, while Solver, an add-in for Excel spreadsheet, is very helpful to optimize models with multiple variables and constraints. For example, in concrete mix design the strength is to be optimised by varying the contents of cement, aggregates, water and pozzolanic materials like fly ash and silica fume. However, to control the cost and to meet the durability and workability requirements the use of cement and water should be within certain limits. These limits have to be the constraints in the concrete optimising models.

Around the world different types of alternative building materials are being developed, particularly there is a big boom in composites and repair materials. These materials have to be tested and evaluated for different properties before their use [2-4]. In building materials research the test data are obtained from various sources such lab experimentation, test machines and data acquisition systems, mainly in the ASCII format, which need to be analysed and presented. This paper illustrates the use of spreadsheets in solving a variety of problems in building materials research activities.

MECHANICAL PROPERTIES

To asses the behaviour of materials under loads various mechanical properties like strength (tensile, compression and flexural), Young's modulus and Poisson's ratio are determined. Most of these properties can be evaluated by plotting load-deformation or stress-strain curves under respective loading configurations. For each test specimen load versus deformation data are generally recorded using either a computerised test machine or by an automatic data logger. The data are then transferred to a spreadsheet. After calculations using this data set the specimen size data a stress-strain curve is obtained for each specimen. For several similar test specimens this becomes a repetitive task. For this purpose a macro can be written or a spreadsheet can be designed. An example is shown in Fig. 1, where the inputs is the load-deformation data and specimen size and output are maximum or ultimate strength and modulus values.

Now-a-days most of the test machines are equipped with computer software which can plot stress-stain curves, but spreadsheets are still useful for combining various curves and presentation of the curves in the desired formats.

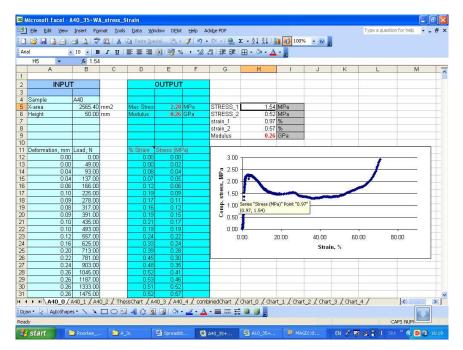


Figure 1 A spreadsheet used for plotting stress-stain curve using data from test machine.

ENERGY ABSORPTION EFFICIENCY

Cellular materials, like foams undergo a large deformation before complete crushing. This property of these materials is exploited for several energy absorption applications, like helmets, crash barriers, motor vehicles and aerospace structures. The energy absorption up to any strain (ε) can be obtained by integrating the area under the stress-strain curve up to that strain. There are various methods adopted for evaluating characteristics and selection of a suitable energy absorbing material for a given application. These methods include: (i) energy absorption capacity (ii) energy absorption efficiency and (iii) energy absorption diagram. '*Energy absorption efficiency* (η)' is a convenient parameter. It can be defined as the percentage ratio of energy absorbed by a real material to that of an ideal energy absorber at a given strain (ε) and can be expressed as following [5]:

$$\eta = \frac{\int \sigma d\varepsilon}{\sigma_{\max} \varepsilon} \times 100 \tag{1}$$

where σ_{max} is the maximum stress recorded up to the strain ϵ . Thus, an ideal energy absorber shows a rectangular stress-strain curve until maximum permissible deformation, while brittle materials have negligible area after the peak. A typical curve showing change in energy absorption efficiency is presented in Fig.2 and the spreadsheet computations of various parameters are shown in Fig 3. In this spreadsheet the inputs are same as they were for the spreadsheet used for stress-strain curve shown in Fig. 1.

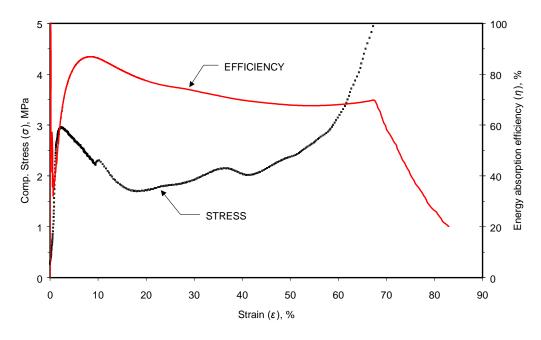


Figure 2 Compressive stress-strain curve and energy absorption efficiency.

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Figure 3 Spreadsheet computation of energy absorption efficiency.

SPECIFIC SURFACE AREA OF PARTICLES

In making concrete and composites various aggregate and particulate materials like fly ash, red mud, calcium carbonate and talc powder are used. Their specific surface area is one of the

important characteristics that determine the binder requirement, the bond between the particles and the binding matrix and for various other reasons [6]. Fig. 4 shows a spreadsheet programme to determine the surface area of particulate materials using Gates Diagram method. As can be seen the inputs are sieve analysis data, specific gravity or the particle density and a constant of proportionality. The value of the constant of proportionality depends upon the geometrical features of the particles. For blocky irregular shapes the value is 12.

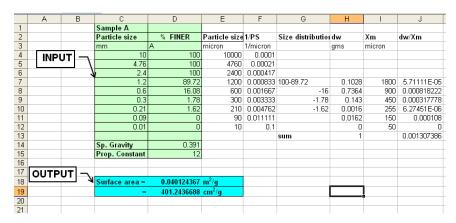


Figure 4 Spreadsheet for determining surface area of particulate materials.

MIX DESIGN

Concrete has been an integral part of the buildings since the beginning of the 20th century. Its properties depend upon the proportion and quality of the constituent materials. The critical factors are the cementitious material and water content. In cementitious materials, besides Portland cement, pozzolanic materials like silica fume, fly ash, slag and metakaolin are also added to improve performance and durability of concrete. The value of water-cement (w/c) ratio is kept as low as possible to achieve high strength and durability. Use of spreadsheets for optimisation of concrete mixes has been presented by Kasperkiewicz [7] and a method of design of trial mixes to determine the quantities of different ingredients using formulae without the use of any charts or tables has been described by Ganju [8].

In concrete mix designs and in use of powders in making composites, the role of particle packing is crucial. This can be achieved by proper selection of aggregates/particles type and particle size distribution. The optimum composition of an aggregate mix can be determined either by using "ideal" grading curves or by means of theoretical and practical determination of aggregate packing value [9]. There are different types of "ideal" curves available such as Bolomey's, Fuller's, Graf's, Rissel's curves, which were obtained by practical experiments and theoretical calculations.

Spreadsheet calculations were used for obtaining an optimal mix of the three different size cork granules of particle size distribution curves shown in Fig 5 [10]. On the same chart a Fuller's curve for an ideal grading obtained by the following equation was drawn.

$$X_{i} = \sqrt{\frac{d_{i}}{d_{\max}}}$$
(2)

where X_i is the ideal percentage finer or passing, d_i is particle size and d_{max} is the largest particle size. In the present research d_{max} was 4.76 mm. The optimum mix was determined as large size

(49.6 %), medium size (28.9%) and small size (21.5%). The real mix using this composition is also shown in Fig. 5, which is quite close to the Fuller's curve.

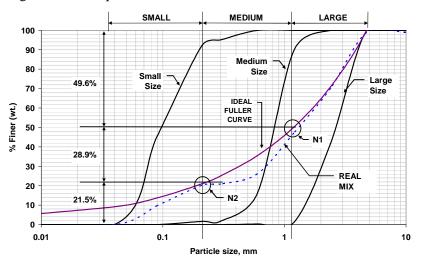


Figure 5 Optimisation of particle grading using Fullers curve.

HEAT OF HYDRATION

Cement is an important building material. When it is mixed with water heat is librated, which indicates setting of cement. Measurement of the heat evolution is useful to understand hydration behaviour of cement, its raw material formulation and its interaction with other ingredients in concrete like materials. In semi-adiabatic technique the hydration tests can be performed in Dewar flasks, where the hydration temperature of each cement-water mix is recorded with the aid of thermocouples connected to a multipoint data recorder. Each sample for the hydration test is prepared by thoroughly mixing cement and admixture, if any, in a plastic bag. The required amount of water is then added and mixed for 2 minutes. A thermocouple is attached to the bag for measuring the temperature change of the mix. The plastic bag is then placed in a Dewar flask for a certain period generally 24 hours. For each replication, a different flask is used so that any possible experimental error could be minimised. All the hydration experiments are carried out in a temperature controlled room. Further details can be seen in [11].

A considerable amount of calculations are required for determination of rate of heat evolution and total heat evolution. For this purpose both numerical differentiation and integration are required. Further details of the calculations can be seen elsewhere [11]. In heat of hydration determination the other important parameters are the values of maximum temperature and maximum heat evolution rate and their corresponding time. For this purpose there is no need to manually check the values. A built in function in Excel spreadsheet can be used as shown in Fig. 7.

For maximum value the Excel spreadsheet function is:

= MAX(B3:B95)

and for the corresponding value of time in column A is:

=INDEX(\$A\$3:\$A\$95,MATCH(MAX(B3:B95),B3:B95,0))

The rate of heat evolution (Q_i) , at any instance t_i , was calculated from the following relationship:

$$Q_i = \frac{dH_i}{dt_i} = \left(C_c + C_f\right) \left(\frac{d(T_i - T_r)}{dt_i} + k\left(T_i - T_r\right)\right)$$
(3)

where C_c is the heat capacity of the contents, C_f is the heat capacity of the Dewar flask and k is cooling rate constant. The total heat evolved up to any instance t_i was obtained by integrating the rate of heat evolution with respect to time:

$$H_i = \left(C_c + C_f\right) \left(\left(T_i - T_r\right) + \sum_{0}^{i} k \left(T_i - T_r\right) dt \right)$$
⁽⁴⁾

Spreadsheets were also used to obtain the values for the heat of hydration using a maturity function by numerically differentiating the total heat with respect to both, the real time and the 'equivalent time', calculated using equation (5) at a reference temperature generally 20 °C. The value of t_{emax} is obtained from the rate of heat evolution curve based on 'equivalent time' determined using a maturity function proposed by Freiesleben Hansen and Pedersen [12] to compute the equivalent age of concrete, which was based on the Arrhenius equation. This maturity function can be applied to determine the 'equivalent age' (t_e) of various hydration samples that undergo different temperature histories. The following relationship gives the 'equivalent age' at any instance *i*.

$$t_e = \sum_{0}^{i} e^{\frac{-E_a}{R} \left(\frac{1}{T} - \frac{1}{T'}\right)} dt$$
⁽⁵⁾

Where ' E_a ' is the apparent activation energy of cement (J/mol), R is the gas constant (8.314 J/mol-K), T and T' are absolute specimen and reference temperatures (Kelvin), respectively.

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5	8	45.6	40.9	36.3	42.2	40	39.7	42	37.8	40.8		8	43.27	39.57	38.
6	8.25	46.2	41.4	36.6	42.9	40.3	40.3	42.6	38.3	41.2		8.25	43.90	40.00	39.
7	8.5	46.8	42	37.1	43.4	40.9	40.6	43.2	38.7	41.6		8.5	44.47	40.53	39.
3	8.75	47.1	42.3	37.2	43.8	41.4	40.8	43.9	39.2	42		8.75	44.93	40.97	40.
9	9	47.6	42.7	37.7	44.3	41.5	41.2	44.2	39.4	42.3		9	45.37	41.20	40.
)	9.25	47.8	42.8	37.9	44.5	42	41.4	44.6	39.9	42.5		9.25	45.63	41.57	40.
1	9.5	48	43.3	38.2	44.8	42.2	41.6	44.9	40.1	42.6		9.5	45.90	41.87	40.
2	9.75	47.9	43.4	38.2	45	42.4	41.9	45.1	40.3	42.8		9.75	46.00	42.03	40
3	10	47.8	43.7	38.4	44.8	42.4	41.9	45.1	40.4	43.1		10	45.90	42.17	41
4	10.25	47.9	43.7	38.6	45.1	42.6	42	45.3	40.6	42.9		10.25	46.10	42.30	41.
5	10.5	47.7	43.7	38.5	44.8	42.5	42.2	45.3	40.7	43		10.5	45.93	42.30	41
3	10.75	47.5	43.7	38.6	44.9	42.7	42.1	45.3	40.6	43		10.75	45.90	42.33	41
7	11	47.1	43.9	38.7	44.6	42.6	42.1	44.9	40.6	43.1		11	45.53	42.37	41
3	11.25	46.8	43.7	38.6	44.4	42.6	42.2	44.8	40.6	43		11.25	45.33	42.30	41
9	11.5	46.3	43.6	38.6	44.2	42.5	42	44.7	40.3	42.9		11.5	45.07	42.13	41.
0	11.75	46	43.6	38.4	43.9	42.3	41.9	44.4	40.5	42.8		11.75	44.77	42.13	41.
1	12	45.5	43.7	38.3	43.6	42.1	42	44.1	40.3	42.9		12	44.40	42.03	41
5	20.5	31.6	34.1	31.1	31.7	32.6	33.4	31.8	31.6	33.9		20.5	31.70	32.77	32.
6	20.75	31.2	33.8	31	31.6	32.6	33.4	31.6	31.5	33.7		20.75	31.47	32.63	32.
7	21	31	33.5	30.9	31.3	32	33	31.2	31.4	33.7		21	31.17	32.30	32.
В	21.25	30.9	33.4	30.7	31.1	32	32.9	31	31.1	33.5		21.25	31.00	32.17	32.
9	21.5	30.7	33.1	30.5	30.8	31.6	32.8	30.9	30.9	33.1		21.5	30.80	31.87	32.
D	21.75	30.2	32.6	30	30.3	31.6	32.4	30.5	30.7	32.9		21.75	30.33	31.63	31.
1	22	30.2	32.5	30	30.4	31.2	32.1	30.5	30.5	32.6		22	30.37	31.40	31.
2	22.25	30	32.3	29.8	30.2	31	32.1	30	30	32.3		22.25	30.07	31.10	31.
3	22.5	29.7	32.1	29.6	30	30.9	31.6	29.7	29.8	32.1		22.5	29.80	30.93	31.
4	22.75	29.3	31.8	29.4	29.5	30.6	31.7	29.6	29.7	31.8		22.75	29.47	30.70	30.
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Figure 6 Spreadsheet for evaluating heat of hydration parameters.

THERMAL CONDUCTIVITY MEASUREMENT

Thermal conductivity (λ) is a measure of the ability of a material to conduct heat through it. A low value of λ is desirable for a material like lightweight concrete when it is used for thermal insulation purposes. Several foams and mineral wools are also used for thermal insulation purposes. A material having a low value of λ can provide the same thermal insulation with a thinner wall than a material having a high value of λ . Thus, thermal conductivity has both structural and economic effects on building designs.

The arrangement of a test set-up for a dynamic method of thermal conductivity measurement is discussed in [10]. In this method the test specimen is sandwiched between two thin aluminium plates. The lower plate is heated from the bottom by a hot plate and the upper plate was allowed to cool from the top in a room with a controlled temperature. This assembly is insulated on the sides and bottom by a low-density polystyrene foam to allow one dimensional heat flow through the specimen. The temperatures at the inner surface (T_1) and outer surface of the specimen (T_2) are recorded at small intervals with the help of thermocouples and a data recorder.

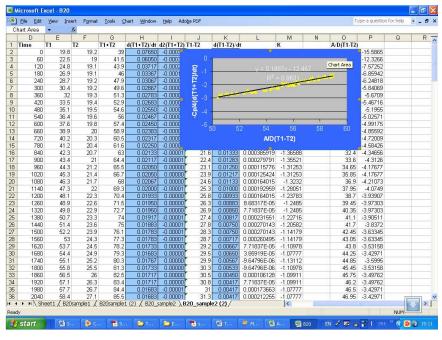


Figure 7 Spreadsheet for determination of thermal conductivity.

If at any instance (t_i) , the rate of heat supplied to the sample is Q_1 , the rate of heat going out of the sample is Q_2 and the rate of heat retention within the sample is Q_3 . Then the relationship can be expressed as:

$$\frac{\lambda A(T_1 - T_2)}{D} - Q_1 = -\frac{C_p}{4} \frac{d(T_1 + T_2)}{dt}$$
(6)

where, C_p be the thermal capacity of the sample, T_1 is the temperature near the heat source and T_2 is the temperature near the heat sink, D is the thickness (m) and A is the area (m²) of the specimen and λ is the thermal conductivity of the specimen. Now considering that the heat supply

is constant and if the values of $-\frac{C_p}{4}\frac{d(T_1+T_2)}{dt}$ are plotted against values of $\frac{A(T_1-T_2)}{D}$, then

the slope of the line will give the value of thermal conductivity and the intercept will be the rate of heat input (Q_I) . An example of the use of spreadsheet for these calculations is shown in Fig. 7.

STATISTICAL ANALYSIS

In spreadsheets various statistical functions are available, which can be used for statistical analysis of the experimental data. An example of Analysis of Variance (ANOVA) for multiple comparison of the CM Factor, a parameter used for assessing wood-cement compatibility, is shown in Fig. 8 [10]. For the post-hoc analysis the Excel Add-In of Keller [13] were used because Excel does not have this function. The results were comparable with those obtained from the commercial statistical software.

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35	MOLO			HDSS	0.1777	0.0945	-+		0.0868	Sign. Diff.	Sign. Diff.	-	
36 37	MDLS				0.0652	0.0945	-+		0.0868		-		
37 38				LDLS HDSS	0.0319 0.1459	0.0945	-+		0.0868	- Sian Diff	Sign Diff		
39 39	LDMS			LDLS	-0.0334	0.0345			0.0868	Sign. Diff.	Sign. Diff.		
33 40	CDIM3			HDSS	0.0806	0.0945	-+		0.0868				
41	LDLS			HDSS	0.0808	0.0345	-+		0.0868	- Sign. Diff.	- Sign. Diff.		
42	2000				0.1170	0.0040			0.0000	sign part.	olgn. colt.		
43													
	Conclus	ion MF	nMS a	nd I DMS ar	e significant	ly different, b	ut MD	I S and I	D are not	I However F	is significar	J ntlu different	with all at
						s not make e							
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44 45						UTEN 4	onż.	/ 200	6 / 20	nor. /			
45	()))	Λcm	IFAC'	tor / Mi	JLT4 🗶 M		U*70	6 <u>CUP</u>	ים גיסי				
45 •		∖ cm	IFAC	TOR / MI	JLT4 (M		.U%	<u> 7</u> 209	ο <u>γ</u> οι	J70 J			
1 5		∖_см	IFAC	TOR (M	JLT4 <u>(</u> M		.U%o	χ 209	0 / 30	J70 7			

Figure 8 Statistical analysis for multiple comparison of samples in spreadsheet

CONCLUSION

The paper demonstrates that spreadsheets have wider applications in building materials research, which include import and export of experimental data; evaluation of mechanical properties, surface area, heat of hydration, thermal conductivity; optimisation of mixes and particle grading and statistical analysis. The use of spreadsheets is very convenient, but has some limitations in plotting charts and in statistical analysis, which can be supplemented with Add-Ins.

ACKNOWLEDGEMENT

The author thanks the Director, CBRI, Roorkee for grant of permission to present this paper.

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